

Resonances and mode shapes of the human vocal tract during vowel production

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Outline

① Intro

Phonetics

Data acquisition

② Models

Big Picture

Helmholtz model

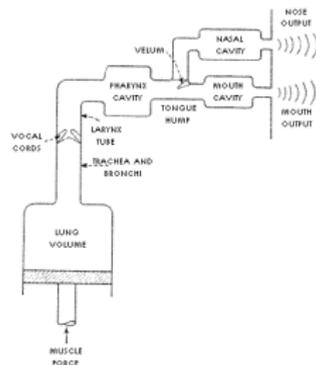
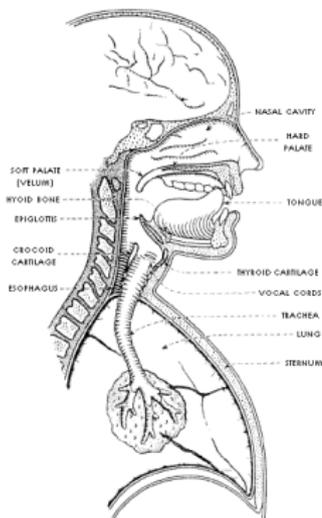
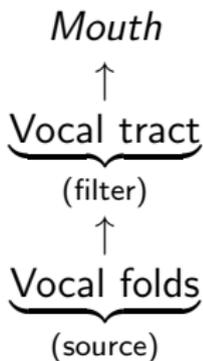
Webster resonator

③ Results

④ Conclusion

Human voice production

Vowel production:



Flanagan, J. L. (1972). *Speech Analysis Synthesis and Perception*, Springer-Verlag.

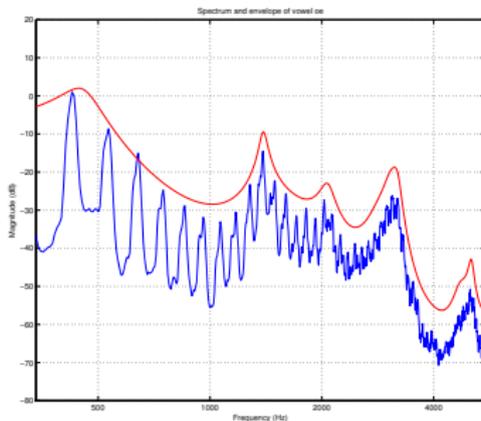
Other speech sounds:

- Vocal tract (VT) shape changes.
- Sound sources vary depending on the speech sound.

Formants

Definition

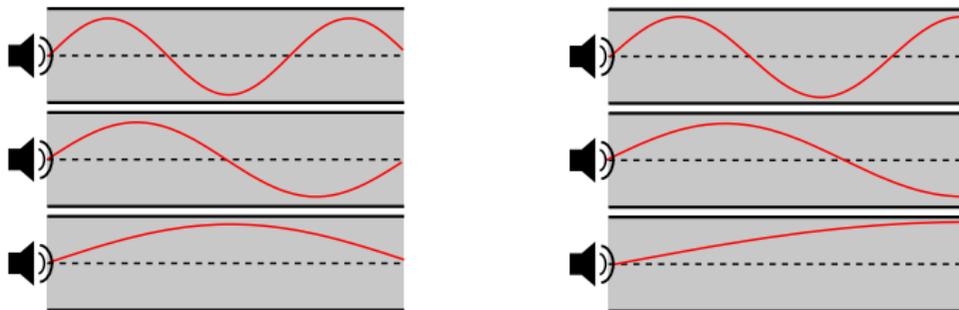
Formants are the envelope peaks of the sound spectrum.



Resonances and formants

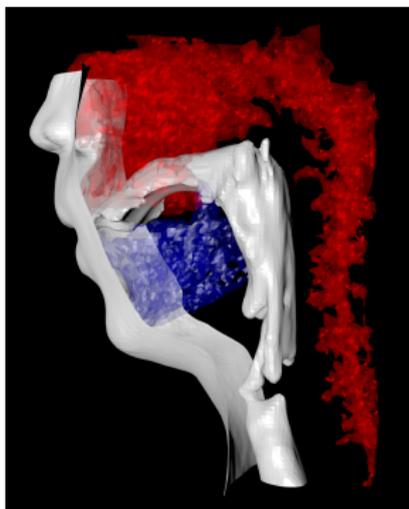
Definition

Resonances are computationally determined resonance frequencies for the VT.

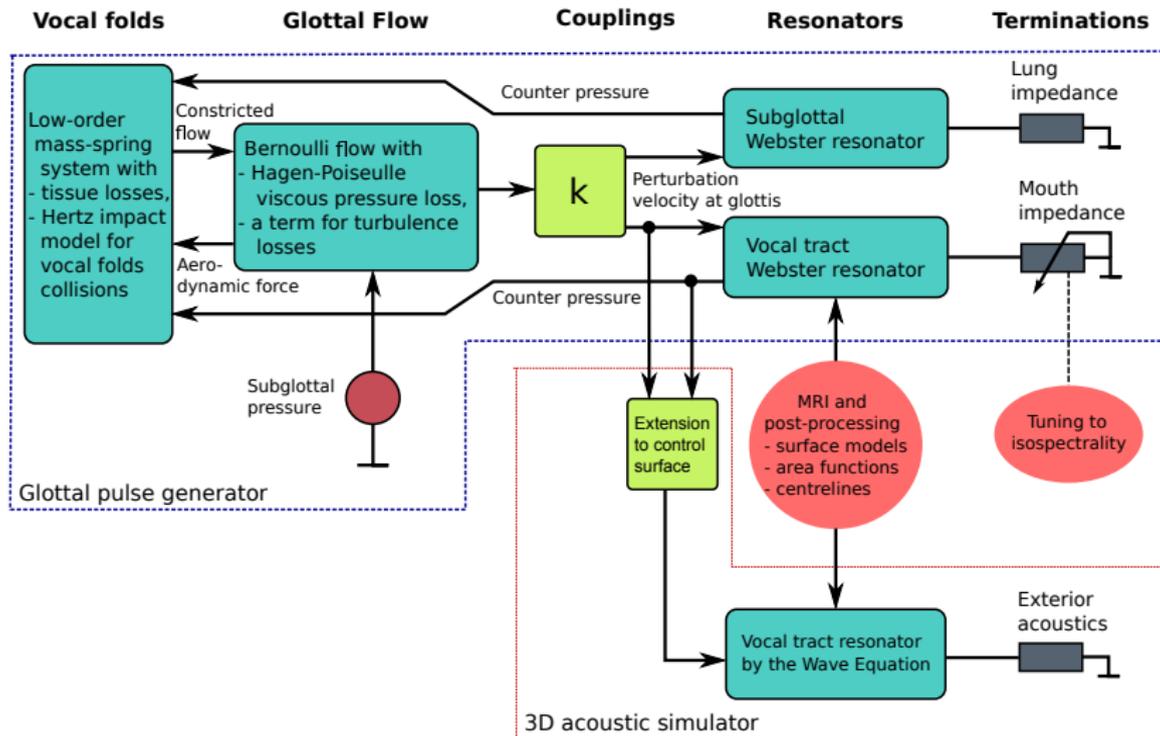


Data acquisition

- Simultaneous speech recording during 3D MR imaging.
- Formants are determined from the speech recordings after noise cancellation.
- Geometry for the computational model is constructed from MR images.



The models



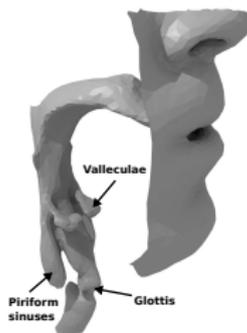
Helmholtz model

$$\begin{cases} \lambda^2 \Phi_\lambda = c^2 \Delta \Phi_\lambda \\ \Phi_\lambda = 0 \\ \frac{\partial \Phi_\lambda}{\partial \nu} = 0 \\ \lambda \Phi_\lambda + c \frac{\partial \Phi_\lambda}{\partial \nu} = 0 \end{cases}$$

in VT volume Ω
on mouth opening Γ_1
on VT walls Γ_2
on vocal folds Γ_3 ,

(1)

- Φ_λ the velocity potential
- c the speed of sound
- ν exterior normal



Helmholtz model 2

The variational formulation of (1) is

$$\lambda^2 \int_{\Omega} p_{\lambda} \phi \, d\Omega + \lambda c \int_{\Gamma_3} p_{\lambda} \phi \, d\omega + c^2 \int_{\Omega} \nabla p_{\lambda} \cdot \nabla \phi \, d\Omega = 0. \quad (2)$$

Using FEM with piecewise linear shape functions and a tetrahedral mesh with approximately 10^5 elements, we construct matrices \mathbf{K} , \mathbf{M} and \mathbf{P} . Equation (2) can then be written as a quadratic eigenvalue problem

$$\lambda^2 \mathbf{K} \mathbf{x}(\lambda) + \lambda c \mathbf{P} \mathbf{x}(\lambda) + c^2 \mathbf{M} \mathbf{x}(\lambda) = 0.$$

This corresponds to the generalized eigenvalue problem

$$\begin{bmatrix} -c\mathbf{P} & -c^2\mathbf{M} \\ \mathbf{I} & 0 \end{bmatrix} \mathbf{y}(\lambda) = \lambda \begin{bmatrix} \mathbf{K} & 0 \\ 0 & \mathbf{I} \end{bmatrix} \mathbf{y}(\lambda), \quad \text{where} \quad \mathbf{y}(\lambda) = \begin{bmatrix} \lambda \mathbf{x}(\lambda) \\ \mathbf{x}(\lambda) \end{bmatrix}$$

Webster resonator

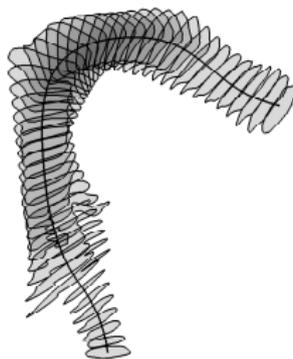
$$\lambda^2 \psi_\lambda = \frac{c^2 \Sigma(s)^2}{A(s)} \frac{\partial}{\partial s} \left(A(s) \frac{\partial \psi_\lambda}{\partial s} \right) \quad \text{for } s \in [0, \ell], \quad (3)$$

ψ_λ velocity potential

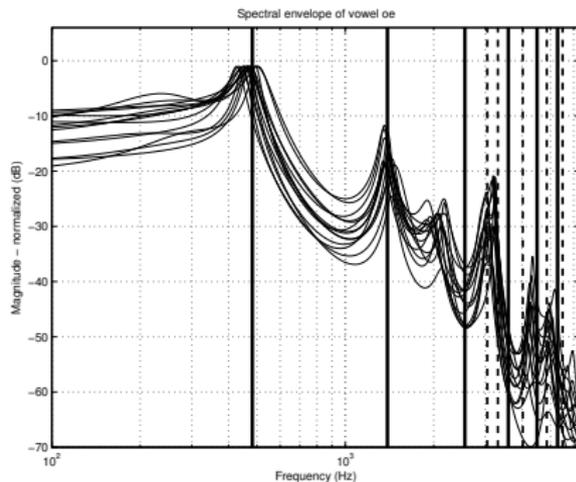
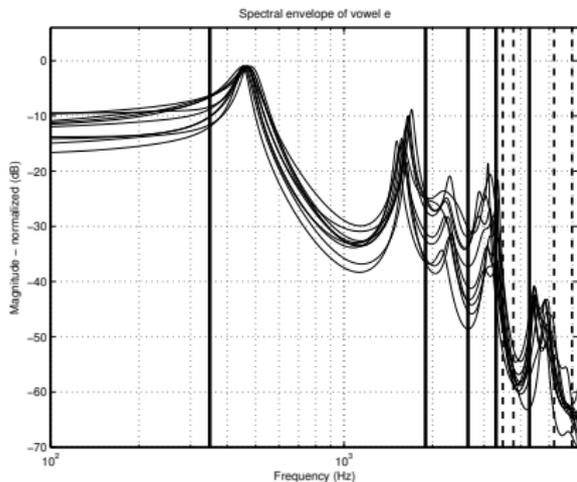
c speed of sound

$A(s)$ area at s

$\Sigma(s)$ curvature correction



Resonances and formants for e and oe



- As expected, different models somewhat corresponds.
- Helmholtz resonances form clusters.

Mode shapes for e

e R1 = 355.5282



e R2 = 1961.9912



e R3 = 2802.2178



e R4 = 3383.439



e R5 = 3474.4559



e R6 = 3771.8868



e R7 = 4248.7415



e R8 = 5193.8313



Mode shapes for oe

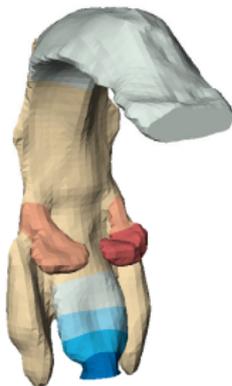
oe R1 = 490.4197



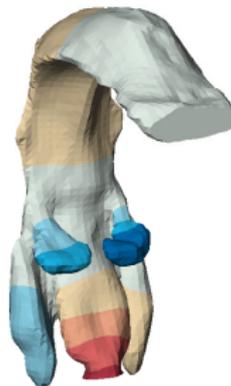
oe R2 = 1422.4823



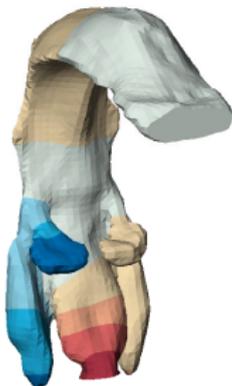
oe R3 = 2626.1411



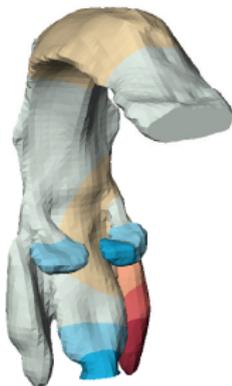
oe R4 = 3047.1356



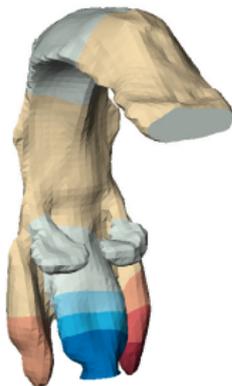
oe R5 = 3311.222



oe R6 = 3487.431



oe R7 = 4030.652



oe R8 = 4865.4169



Classifying resonances

- Helmholtz resonances are complicated.
 - The resonance direction is not well defined.
 - There are Transversal components (the clusters).
- Webster model only capture longitudinal resonances.
 - The resonances "average" the clusters of the Helmholtz resonances.
 - There is no one-to-one correspondence.
- At least the longitudinal resonances show up as formants.
 - The LPC algorithm also does some "averaging".
 - There are other sources of error.
- There's some discrepancy between formants and resonances .
 - The unrealistic mouth boundary condition is a likely cause.

Conclusions

- The VT can have significant transversal resonances.
 - Most articulatory models only consider longitudinal resonances.
 - Trained singers are known to be able to produce formants not visible in the spectra of untrained singers.
- A more realistic acoustic impedance at mouth should give better results.
 - Modelling of the exterior space is an ongoing project.
- Full classification of the resonance structure requires going through a larger set of data.
 - Dimensions of the vocal space.

The End

Questions?

<http://speech.math.aalto.fi>